Artificial neural network based modeling and controlling of distillation column system

Totok R. Biyanto¹,⁴*, Bambang L. Widjiantoro¹, Ayman Abo Jabal², Titik Budiati³

¹ Engineering Physic Dept. - FTI – ITS Surabaya, INDONESIA
² College of Engineering, Sudan University of Science & Technology (SUST), SUDAN
³ School of Industrial Technology - Universiti Sains Malaysia, MALAYSIA
⁴ Universiti Teknologi PETRONAS, MALAYSIA

*Corresponding Author: e-mail: trb@ep.its.ac.id, Tel +62 31 5947188 Fax. 62 31 5982806

Abstract

A Neural Network Internal Model Control (NN-IMC) strategy is investigated, by establishing inverse and forward model based neural network (NN). Further for developing the model has been selected suitable adaptive filter. Two types of NN-based inverse model (i.e. with and without disturbance input) were accurately simulated. The results indicated that the neural networks are capable to establish forward and inverse model rapidly from the couple of input-output open loop data of single distillation column binary system with a good root mean square error (RMSE). The simulation results revealed that NN-IMC with appropriate learning rate - momentum is capable to pursue the set-point changes and to reject the disturbance changes without steady state error or oscillations. NN-IMC with inverse model which contains disturbance input (modified NN-IMC) offer better performance than without it (conventional NN-IMC).

Keywords: Neural network, modeling, control, modified internal model control (IMC), distillation column

1. Introduction

Predictive control is currently one of the most widely used advanced control methods in industry, especially in the control of processes that are protected, multivariable and uncertain. A great number of implementation algorithms, including industrial predictive control applications (Qin et al., 2003) have frequently in the literature. Distillation is one of the most essential processing units in chemical engineering and petroleum refining, and it required to be controlled near to the optimum operating conditions as a consequence of economic incentives. The purpose of a distillation column is to separate a mixture of components into two or more products of different compositions. The physical approach of separation in distillation is the difference in the volatility of the components. The separation occurs in a vertical column where heat is added to a reboiler at the bottom and removed from condenser at the top. A stream of vapor produced in the reboiler rises through the distillation column and is forced into contact with a liquid stream from the condenser flowing downwards in the column. The volatile (light) components are enhanced in the vapor phase and the less volatile (heavy) components are enriched in the liquid phase. A product stream taken from the top of the column therefore mainly contains light components, whereas a stream taken from the bottom contains heavy components (Kanthasamy, 2009). The majority of the industrial distillation columns are currently controlled by multiloop controllers based on linear models which are penalized by several shortcomings. Nonlinear model based control system is one of the unique options to be explored for proper control of distillation columns. Furthermore, distillation column is used in industry as multivariable, nonlinear and complex processes. Extractive distillation is a separation process used to separate the binary mixture methanol-water by differences of volatility. Control structure of liquid flow rate at reflux and vapor boilup flow rate at reboiler (LV) are the best control pairing in binary distillation column system. Mole fraction of distillate and bottom product maintained respectively by regulate reflux flow rate & steam flow rate (Skogestad et al, 1990).

Most promising application areas of the neural network control are robotics, process control, vehicle guidance and teleoperation. A good introduction to the subject is given in the books . Neural Networks for Control. (ed. Miller, Sutton and Werbos, 1990) and
Artificial neural networks can be used in several fields of control engineering: as process models, as controllers, for optimization and failure detection. Previous work (Garcia et al., 1986) refers to Model Predictive Control (MPC) as type of controllers in which there is a direct use of explicit and separate identifiable model. The same process model is implicitly used to compute the control action in such a way that the control design specifications are satisfied. Control design methods based on MPC concept have found wide acceptance in industrial applications due to their high performance and robustness. There are several variants of model predictive control methods, like Dynamic Matrix Control (DMC), Model Algorithmic Control (MAC) and Internal Model Control (IMC). Also nonlinear versions of these are developed, for example the nonlinear IMC concept. (Chen et al., 1994) A largely independently developed branch of MPC, called Generalized Predictive Control (GPC), is aimed more for adaptive control. For the current state-of-the-art of MPC (Clarke et al., 1989). For NN-IMC, nevertheless, even though the NN model is available, it is complicated to design the NN inverse controller owing to the following reasons. First, the process required to be controlled, must be stable in open-loop, which certainly limits many of IMC applications (Saint-Donat et al., 1991; Willis et al., 1992). Second, the process to be controlled is required to have stable zero dynamics because of the use of the model inversion. For our understanding, little consequence has been reported about the NN-IMC of nonlinear non affine discrete systems with unstable zero dynamics. Third, it may not be easy to have the model inversion for control law design due to the nonlinear internal model used.

For the third problem mentioned previously, some solutions are introduced under certain conditions. One of the solutions is to train an NN inverse controller with the help of the identified NN model (Rumelhart et al., 1986, Baguman et al., 1990) If a nonlinear-in-the parameters type model is applied for adaptive control in a way analogous to the linear self-tuning scheme, one must accept that start-up behavior comparable to the linear case is not typically obtained and that all operation points should be visited at least once before good control performance is achieved. A minor off-line identification is of course a solution to the problems encountered during the initial start-up phase. This reduces the effect of randomly selected initial weights. (Rivals et al., 2000). The neural networks application in chemical engineering field offers potentially effective means of handling three difficult problems: Complexity, non-linearity and uncertainties. The variety of available neural network architectures authorizes us to deal with a wide range of process control problems in comparison with other empirical models. Neural networks are relatively less sensitive to noise and incomplete information and deal with higher levels of uncertainty when applied in process control problems (Hunt et al., 1991).

There are several results of research concerning the Neural Network – Internal Model Control (NN-IMC), which are implemented on different process (Rivals et al., 2000, Changjie et al., 2005, Varshney et al., 2009). These papers show that the advantages of Internal Model control systems are their robustness with respect to a model mismatch and to disturbances. In another paper, the NN-IMC was compared with conventional control (PID). It is shown that the NN-IMC has better performance than PID controller (Alarçin, 2007). The objective of this paper is to obtain faster response performance in controlling binary distillation column using modified NN-IMC. The proper structure of NN model inverse and forward model, proper filter, and on-line training is needed. Multilayer feed forward neural networks with back propagation algorithm have been utilized for modeling in MATLAB and distillation column is modeled in HYSYS. Comparison of ANN based control schemes are illustrated using error analysis.

2. Distillation Column NN-IMC Control System

2.1 Distillation Column

The column contains a total of $N_T$ theoretical trays. The liquid hold up on each tray including the down comer $M_N$. The liquid on each tray is assumed to be perfectly mixed with composition $X_N$, showing in Figure1, the mathematical formula expressing the process in the distillation column using rigorous modeling described as follows (Luyben, 1990):

Nth tray

Mass balance:

$$\frac{dM_N}{dt} = L_{N+1} - L_N + V_{N-1} - V_N$$  \hspace{1cm} (1)

Component mass balance:

$$\frac{d(M_N X_N)}{dt} = L_{N+1} X_{N+1} - L_N X_N + V_{N-1} Y_{N-1} - V_N Y_N$$  \hspace{1cm} (2)

Energy balance:

$$\frac{d(M_N h_N)}{dt} = L_{N+1} h_{N+1} - L_N h_N + V_{N-1} H_{N-1} - V_N H_N$$  \hspace{1cm} (3)
2.2 Condenser and reflux drum

The overhead vapor totally condensed in a condenser and flows into the reflux drum, whose holdup of liquid is \( M_D \) (moles). The content of the drum is at its bubble point. Reflux is pumped back to the top tray (NT) of column at a rate \( L \). Overhead distillate product is removed at a rate \( D \).

Mass balance:

\[
\frac{dM_D}{dt} = V_{NT} - L_{NT+1} - D \tag{4}
\]

Component mass balance:

\[
\frac{d(M_D X_D)}{dt} = V_{NT} Y_{NT} - (L_{NT+1} + D) X_D \tag{5}
\]

Energy balance:

\[
\frac{d(M_D h_D)}{dt} = V_{NT} H_{NT} - L_{NT+1} h_{NT+1} - D h_D - Q_c \tag{6}
\]

2.3 Reboiler and base column

At the base of the column, liquid bottoms product is removed at a rate \( B \) and with composition \( X_B \). Vapor boil up is generated in thermosiphon reboiler at rate \( V_B \). Liquid circulates from the bottom of the column through the tubes in the vertical tube-in shell reboiler because of the smaller density of the vapor liquid mixture in the reboiler tubes. We will assume that the liquids in the reboiler and in the base of the column are perfectly mixed together and have the same composition \( X_B \) and total holdup \( M_B \) (moles). The composition of the vapor leaving the base of the column and entering tray 1st is \( y_B \). It is in equilibrium with the liquid with composition \( X_B \).

Mass balance:

\[
\frac{dM_B}{dt} = L_1 - V_B - B \tag{7}
\]
Component mass balance:
\[
\frac{d(M_B X_B)}{dt} = L_1 X_1 - V_B Y_B - B X_B
\]  
(8)

Energy balance:
\[
\frac{d(M_B h_B)}{dt} = L_1 h_1 - V_B h_B - B h_B + Q_R
\]  
(9)

Feed tray (N = NF)
A single feed stream is fed as saturated liquid onto the feed tray NF. Feed flow rate is F (mole/hour) and composition X_F (mole fraction more volatile component).

Mass balance:
\[
\frac{dM_{NF}}{dt} = L_{NF+1} - L_{NF} + F + V_{NF-1} - V_{NF}
\]  
(10)

Component mass balance:
\[
\frac{d(M_{NF} X_{NF})}{dt} = L_{NF+1} X_{NF+1} - L_{NF} X_{NF} + V_{NF-1} Y_{NF-1} - V_{NF} Y_{NF} + F_z X_F
\]  
(11)

Energy balance:
\[
\frac{d(M_{NF} h_{NF})}{dt} = L_{NF+1} h_{NF+1} - L_{NF} h_{NF} + V_{NF-1} h_{NF-1} - V_{NF} h_{NF} + F h_F
\]  
(12)

2.4 NN-IMC (Neural Network-Internal Model Control)

The internal model control (IMC) scheme has been widely applied in the field of process control. This is due to its simple and straightforward controller design procedure as well as its good disturbance rejection capabilities and robustness properties. An Internal Model Control System (IMC) is presented in Figure 2. It consists of a collection of interconnected blocks: model, comparator, corrector, and controller. The model consist of controller model (Gc), plant model (Gp), forward model (Gm) and disturbance model (Gu). Basically in this structure, a feedback signal, result of a comparison between the actual process output Y and the model output of the process Ym to be controlled, is used to correct the reference signal (R). The feedback signal is active when a disturbance (U) acts on the process or the process and model behaviors are different.

The IMC scheme has two interesting characteristics:

- While modeling is accurately achieved, nominal tracking dynamic of the comprehensive system in absence of disturbance is reduced to that of the compensated process. The global system function is open loop.
- Significant functioning is obtained even using a poor model. Generally, if the static gain of the compensated model is unity; full rejection of disturbance is achieved in steady state condition.

The first characteristic implies that the process to be controlled must be stable. Accurate modeling of the process is not necessary thanks to the fairly significant robustness of the IMC scheme and approximate models of the process can often be satisfactory. Therefore a reduced amount of information about the process, such as the rise-time and the static gain, can be sufficient. Traditionally, internal models were implemented using mathematical equations. The structure of the model that was chosen could
use some previous knowledge of the plant, and the parameters obtained by an identification procedure. In some cases real time identification was used and the parameters of the model modified during the functioning of the system. The idea, here, is to use Internal Models implemented using NN in view of representing the knowledge of the control of the considered process. This is made possible because the internal model approach does not rely on an explicit mathematical model of the plant.

Neural networks are information processing systems. Neural networks can be thought of as “black box” devices that accept input and produce output. Each neural network has at least two physical components: connections and processing element (neuron). The combination of these two components creates neural networks. In a broad sense, an artificial neural network diagram is consisting of three principal elements:

- Topology – how a neural network is organized into layers and how those layers are connected.
- Learning – how information is stored in the network.
- Recall – how the stored information is retrieved from the network.

In system identification view point, the advantages of neural networks to develop the model are nonlinear system, learning and adaptation, multivariable systems.

Some of the most common neural networks are functional mapping nets like multilayer perceptron (MLP) and cerebellar model articulation computer (CMAC) (Albus, 1975), adaptive resonance nets (ART) that form input categories from input data, input feature categorization nets of Kohonen (Kohonen, 1984), bilinear associative memories and feedback network of analog neurons (Hopfield et al., 1985). An interpolation technique called Radial Basis Functions (RBF) (Moody, et al., 1989, Poggio et al. 1990), is normally viewed as a neural network. Fuzzy models are also an efficient function approximation scheme.

Multilayer perceptron (MLP) is one of the most commonly used neural network architecture today. It constructs an approximation of a multi-input multi-output function in a similar manner as fitting of a low order polynomial through a set of data points. A rich collection of different learning paradigms has been developed. Figure 3 illustrates the example of MLP networks, which consist of input, hidden and output layer.

![Figure 3: Structure of multilayer perceptron](image)

An important and useful feature of MLP networks is that the gradient and various other Jacobians of the model can be computed efficiently in a hierarchical and parallel manner using the chain rule differentiation. This gradient computation method is called the generalized delta rule or error back propagation. (Hopfield et al., 1985) This is commonly considered as a minimization method, i.e. it includes also the steepest descent parameter update. The terms forward pass and backward pass are used in this study to denote the computation of the predictions (forward) and the gradients (backward) only. Common nonlinear least squares methods are Levenberg-Marquardt (LM) and Gauss-Newton (GN).

The MLP network is selected for the basic building block to be used in this study although localized representations have some useful properties over the MLP network. The learning algorithm using LM.

The mathematical formula expressing what is going on in the MLP networks takes the form (Figure 3):

$$ y_k = F \left[ \sum_{j=1}^{n_0} W_{k,j} \left( \sum_{i=1}^{d} \phi_i \phi_1 + w_{j,0} \right) + w_{k,0} \right] = 1, 2, \ldots, C $$

All continuous function can be approximated to any desired accuracy with neural networks of one hidden layer of hyperbolic tangent hidden neuron and a layer of linear output neuron. (Clarke et al., 1989)
3. Design

The first step of design: build the Amplitude Pseudo Random Binary Signal (APRBS), build the structure forward model of neural network for and inverse model of neural network from dynamic data of single distillation column binary system, choose low pass filter and tune gain controller to improve the performance of system. The second step: on-line training and choose an appropriate learning rate and an appropriate momentum in order to NN-IMC produce manipulated variable which make the control variable follow the set-point changes.

3.1 Open loop data for training

![Figure 4](image)

The distillation column operated in open loop condition (inventory control only) in order to obtain its dynamic properties ($X_d$ and $X_b$). Reflux ($L$) and steam reboiler ($Q_r$) regulated according to signal APRBS (Amplitude Pseudo Random Binary Signal). Figure 4 shows the open loop - data which collected and they plotted against time.

3.2 Training of the forward model

Forward model of distillation column is built using NN Multi layer Perceptron (MLP), with input structure Neural Network AutoRegressive (NNARX), which trained by a couple of $L$ and $Q_r$ as input-data and a couple $X_d$ and $X_b$ as output data and by using Levenberg Marquard as learning algorithm. (Figure 4.)
Based on RMSE during training and validation phase, NN-forward model with 6 history lengths (HL) and 13 hidden nodes (HN) is chosen as the best NN structure (Figure 5). As shown in Figure 6 and 7, The RMSE are $5.9908 \times 10^{-5}$ and $1.2686 \times 10^{-4}$ for mole fraction of distillate ($X_d$) and mole fraction of bottom ($X_b$), respectively.

Figure 5: NN forward model architecture

Figure 6: $X_d$ form process and NN model.
3.3 **Training the inverse model**

Similar procedure is applied to train the neural network - inverse model, as well as to train the forward model. The difference is on the inputs-model and on the outputs-model. Inputs of inverse model are $X_d$ and $X_b$ and its outputs are $L$ and $Q_r$, which obtained from training previously. Distillation column data which fed to the model are the past-data and the present-data.

![Figure 7](image)

**Figure 7**: $X_b$ form process and NN model

![Figure 8](image)

**Figure 8**: NN inverse model structure without disturbance input

![Figure 9](image)

**Figure 9**: NN inverse model structure with disturbance input

Figure 8 is inverse model structure without disturbance input (conventional inverse model) and Figure 9 is inverse model structure with disturbance input (modified inverse model). Both of inverse model of distillation column built-up from NN with
Multi layer Preceptor (MLP), Neural Network Auto Regressive, external input structure (NNARX), which trained by L and Qr as output data and Xd and Xb as input data (F and Xf constant and will update at online training) and by using Levenberg Marquard learning algorithm.

![Figure 10: Inverse model validation](image)

NN inverse model has 6 history lengths and 13 hidden nodes and trained for 200 times computer iteration is the best ANN structure to produce good RMSE. Two type NN inverse model have Root Mean Square Error (RMSE) about 0.0483 for L and RMSE about 0.0829 for the Qr. (Figure 10)

### 3.4 On Line Training

The IMC control strategy required the inverse model as well as the forward model. IMC uses the forward model to compare with the process output and the deviation is used as one of the input to the inverse model (controller) to produce the better control action. IMC make use of both the inverse and forward model to predict the required control action input to the process. The IMC control strategy incorporates compensation to the inverse model because the output from the system is constantly being comparing with the output of the forward model. Figure 11 shows the control strategy for the Internal Model Control (IMC).

![Figure 11: Online training](image)
The fact the inverse model is a recursive network is ignored during training in the sense that regresor’s dependency on the weights in the network is ignored. The simple training algorithm, which appears in accordance with this approximation, in some sense follows the spirit of so-called recursive pseudo-linear regression methods (PLR).

3.5 Filter

The schematic diagram of NN-IMC for controlling binary distillation column is shown in Figure 12. Low pass filter had been used in this research is chosen by trial and error to filtered high frequency signal and adjusting the controller sensitivity. The filter transfer functions are:

\[
\text{Filter 1} = \frac{1}{s + 0.297229} \quad \text{Filter 2} = \frac{3}{s + 0.297229}
\]

4. Results and discussions

Both of the proposed NN-IMC structure (conventional and modified) are stable and no error steady state. Proposed NN-IMC with inverse model input content of disturbance signal (modified NN-IMC) has better performance compare to NN-IMC without inverse model input content of disturbance signal. Proposed NN-IMC with disturbance input could get information about disturbance changing direct form measurement, so could produce manipulated variable signal early. The result has shown that process variable performance such as Integral Absolute Error (IAE) and settling time getting better.

![Image of Filter Diagram](image)

**Figure 12**: NN-IMC for controlling binary distillation column

Figure 13 shown that \(X_d\) response to the set point of \(X_d\) changes has rise time 187 minute and IAE 2.586 for NN-IMC structure with disturbance input and rise time 403 minute and IAE 4.4519 for NN-IMC structure without disturbance input. Figure 14 shown result of disturbance \(F\) change (increase from 45000 to 45450 gram mole/minute) that trajectory of \(X_d\) response return to the original set point at 266 minute and IAE 1.8133 for NN-IMC structure with disturbance input. Trajectory of \(X_d\) response return to the original set point at 500 minute and IAE 3.1608 for NN-IMC structure without disturbance input.

![Image of Response Diagram](image)

**Figure 13**: Response \(X_d\) proposed NN-IMC when set point \(X_d\) changes.
Table 1: IAE for set point changes

<table>
<thead>
<tr>
<th>No</th>
<th>Set Point (t=500 minute)</th>
<th>IAE NN-IMC With dist. input</th>
<th>IAE NN-IMC Without dist. Input</th>
</tr>
</thead>
<tbody>
<tr>
<td></td>
<td></td>
<td>X_d</td>
<td>X_b</td>
</tr>
<tr>
<td>1</td>
<td>X_d +0.001</td>
<td>2.5860</td>
<td>4.4519</td>
</tr>
<tr>
<td>2</td>
<td>X_d -0.001</td>
<td>3.0235</td>
<td>5.0419</td>
</tr>
<tr>
<td>3</td>
<td>X_b +0.001</td>
<td>2.1026</td>
<td>2.3046</td>
</tr>
<tr>
<td>4</td>
<td>X_b -0.001</td>
<td>2.1151</td>
<td>2.3575</td>
</tr>
</tbody>
</table>

Table 1 shown IAE performance for set point changes and Table 2 shown IAE performance for disturbance changes. From the tables NN-IMC with disturbance input has better performance (IAE) than NN-IMC without disturbance input.

Table 2: IAE for disturbance changes

<table>
<thead>
<tr>
<th>No</th>
<th>Disturbance (t=500 minute)</th>
<th>IAE NN-IMC With dist. input</th>
<th>IAE NN-IMC Without dist. input</th>
</tr>
</thead>
<tbody>
<tr>
<td></td>
<td></td>
<td>X_d</td>
<td>X_b</td>
</tr>
<tr>
<td>1</td>
<td>F+1%</td>
<td>1.8133</td>
<td>11.0866</td>
</tr>
<tr>
<td>2</td>
<td>F-1%</td>
<td>1.8144</td>
<td>13.0649</td>
</tr>
<tr>
<td>3</td>
<td>X_f+1%</td>
<td>1.3694</td>
<td>12.9935</td>
</tr>
<tr>
<td>4</td>
<td>X_f-1%</td>
<td>1.4605</td>
<td>17.3190</td>
</tr>
</tbody>
</table>

5. Conclusions

A forward model and two types of inverse models of binary distillation column have been built using NNARX. The models showed satisfactory performances as evidenced by the lower RMSE values of $5.9908 \times 10^{-5}$ and $1.2686 \times 10^{-4}$ for mole fraction of distillate ($X_d$) and mole fraction of bottom ($X_b$), respectively. The RMSE of two types of inverse models have RMSE of about 0.0483 and 0.0829 for $L$ and $Q_r$, respectively. The models are therefore, ready to use in conventional and modified NN-IMC. Appropriate filters were selected and placed before and after the inverse model. Online training is also required for NN-IMC to obtain a better response in the system for controlling the binary distillation column. The simulation results, both conventional and modified NN-IMC have been found satisfactory. The proposed conventional and modified NN-IMC structures were found to be stable and no error steady state. This is mainly due to the selection of proper open loop data, optimized structure, proper filter, and adaptive inverse model. The inverse model with disturbance signal as input (modified NN-IMC) showed better performances in terms of lower IAE value and faster response as compared with the conventional NN-IMC. Future work will focus on the application of the proposed controller in many plants with difference complexities and characteristics.

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Biographical notes

Totok R. Biyanto is a lecturer in Engineering Physics Department – Industrial Technology Faculty, ITS Surabaya. He has published several papers in various national, international conferences and journals. He has an experience of 15 years as an instrumentation and process control consultant for many industries. Currently working at research & innovation office Universiti Teknologi Petronas, Malaysia.

Titik Budiati is PhD student in School of Industrial Technology, Universiti Sains Malaysia. The scientific field is mathematical modelling.

Bambang L. Widijanto is currently lecturer and Head of the Department of Engineering Physics, Sepuluh Nopember Institute of Technology (ITS) Surabaya, Indonesia. His research area is model predictive control, neural network based control system and process control.

Ayman Abo Jabal received his M.Sc. degree from Czech Technical University Faculty of Technology Zlin in Plastic, Rubber and Leather Technology in 1996. Currently working in the Faculty of Engineering Industrial Technology Department at Sudan University of Science and Technology, His research interests are synthesis polymers material and composite, Rheological property data of Polymer Systems, kinetic reaction for formation and activation energy, thermodynamics.

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